DOCUMENT RESUME

ED 038 305

24

SE 008 252

Shepler, Jack L. AUTHOR A Study of Parts of the Development of a Unit in TITLE Probability and Statistics for the Elementary School, (Part 4) and Appendices B, C, and D. Wisconsin Univ., Madison. Research and Development INSTITUTION Center for Cognitive Learning. Office of Education (DHEW), Washington, D.C. Bureau SPONS AGENCY of Research. TR-105 REPORT NO BR-5-0216 BUREAU NO Nov 69 PUB DATE OEC-5-10-154 CONTRACT 60p. NOTE EDRS Price MF-\$0.50 HC-\$3.10 EDRS PRICE *Curriculum Development, Doctoral Theses, DESCRIPTORS *Elementary School Mathematics, Grade 6. *Instruction, Mathematics Education, *Research,

Statistics

ABSTRACT

Reported is research conducted as a part of the Project on Analysis of Mathematics Instruction. The study had two main purposes: to test the feasibility of teaching topics in probability and statistics to a class of sixth grade students; and to construct a set of instructional materials and procedures in probability and statistics for sixth graders. A unit of instruction was prepared and the order in which behavioral objectives were to be taught was determined from a content outline and a task analysis. The results of the study support the feasibility of teaching most of the topics covered in the unit to average and above average sixth graders. The study also lends support to the use of the systems developmental model employed for developing curriculum materials. Part IV contains Appendices B, C, and D which include the testing instrument used for pre- and post-testing, tables presenting data from the formative evaluation, and background data of the students. (FL)



800

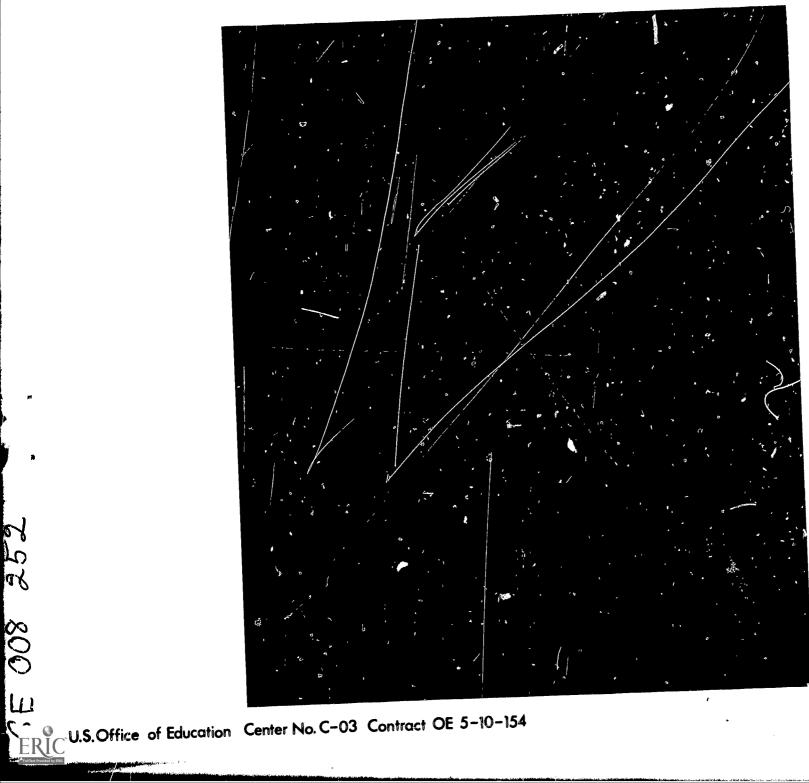
U.S. DEPARTMENT OF HEALTH, EDUCATION & WELFARE OFFICE OF EDUCATION THIS DOCUMENT HAS BEEN REPRODUCED EXACTLY AS RECEIVED FROM THE PERSON OR ORGANIZATION ORIGINATING IT. POINTS OF VIEW OR OPINIONS STATED DO NOT NECESSARILY REPRESENT OFFICIAL OFFICE OF EDUCATION POSITION OR POLICY.

BR 5-0216 PA-24 OE/BR-

No. 105 (Part IV) Appendices B, C, and D rt

> A STUDY OF PARTS OF THE DEVELOPMENT OF A UNIT IN PROBABILITY AND STATISTICS FOR THE ELEMENTARY SCHOOL

Report from the Project on Analysis of Mathematics Instruction



Technical Report No. 105 (Part IV) Appendices B, C, and D

A STUDY OF PARTS OF THE DEVELOPMENT OF A UNIT IN PROBABILITY AND STATISTICS FOR THE ELEMENTARY SCHOOL

Report from the Project on Analysis of Mathematics Instruction

By Jack L. Shepler

Thomas A. Romberg, Assistant Professor of Curriculum & Instruction Chairman of the Examining Committee

Thomas A. Romberg, Principal Investigator

Wisconsin Research and Development Center for Cognitive Learning The University of Wisconsin Madison, Wisconsin November 1969

This Technical Report is a doctoral dissertation reporting research supported by the Wisconsin Research and Development Center for Cognitive Learning. Since it has been approved by a University Examining Committee, it has not been reviewed by the Center. It is published by the Center as a record of some of the Center's activities and as a service to the student. The bound original is in The University of Wisconsin Memorial Library.

Published by the Wisconsin Research and Development Center for Cognitive Learning, supported in part as a research and development center by funds from the United States Office of Education, Department of Health, Education, and Welfare. The opinions expressed herein do not necessarily reflect the position or policy of the Office of Education and no official endorsement by the Office of Education should be inferred.

Center No. C-03 / Contract OE 5-10-154



NATIONAL EVALUATION COMMITTEE

Samuel Brownell

Professor of Urban Education Graduate School Yale University

Launor F. Carter

Senior Vice President on Technology and Development System Development Corporation

Francis S. Chase

Professor Department of Education University of Chicago

Henry Chauncey

President **Educational Testing Service**

Martin Deutsch

Director, Institute for Developmental Studies New York Medical College

Jack Edling

Director, Teaching Research Division Oregon State System of Higher Education

Elizabeth Koontz

President National Education Association

Roderick McPhee

President Punahou School, Honglulu

G. Wesley Sowards

Director, Elementary Education Florida State University

Patrick Suppes

Professor Department of Mathematics Stanford University

*Benton J. Underwood

Professor Department of Psychology Northwestern University

UNIVERSITY POLICY REVIEW BOARD

Leonard Berkowitz

Chairman Department of Psychology

Archie A. Buchmiller

Deputy State Superintendent Department of Public Instruction

*James W. Cleary

Vice Chancellor for Academic Affairs

Leon D. Epstein

College of Letters and Science

John Guy Fowlkes

Director Wisconsin Improvement Program

Robert E. Grinder

Chairman Department of Educational Psychology

H. Clifton Hutchins

Chairman Department of Curriculum and Instruction

Clauston Jenkins

Assistant Director Coordinating Committee for Higher Education Herbert J. Klausmeier

Director, R & D Center Professor of Educational Psychology

Donald J. McCarty

Dean School of Education

Ira Sharkansky

Associate Professor of Political Science

Henry C. Weinlick

Executive Secretary Wisconsin Education Association M. Crawford Young

Associate Dean The Graduate School

EXECUTIVE COMMITTEE

Edgar F. Borgatta Brittingham Professor of Sociology

Max R. Goodson

Professor of Educational Policy

Russell J. Hosler

Professor of Curriculum and Instruction and of Business

*Herbert J. Klausmeier

Director, R & D Center Professor of Educational Psychology

Gary A. Davis

Associate Professor of

M. Vere DeVault

Professor of Curriculum and Instruction (Mathematics)

Educational Psychology

Wayne Otto

Profe or of Curriculum and Instruction (Reading)

Robert G. Petzold

Associate Dean of the School of Education Professor of Curriculum and Instruction and of Music

Max R. Goodson

Professor of Educational Policy

Warren O. Hagstrom

Professor of Sociology

John G. Harvey

and Instruction

Richard L. Venezky Assistant Professor of English

and of Computer Sciences

Richard G. Morrow

Assistant Professor of Educational Administration

Professor of Curriculum and Instruction (Reading)

Professor of Curriculum and

Milton O. Fella

Instruction (Science)

Wayne Otto

FACULTY OF PRINCIPAL INVESTIGATORS

Ronald R. Allen

Associate Professor of Speech and of Curriculum and Instruction

Vernon L. Allen

Associate Professor of Psychology (On leave 1968-69)

Nathan S. Blount

Associate Professor of English and of Curriculum and Instruction

Robert C. Calfee

Robert E. Davidson

Educational Psychology

Assistant Professor of

Associate Professor of Psychology

Frank H. Farley

Assistant Professor of

Educational Psychology

John Guy Fowlkes (Advisor)

Professor of Educational Administration

Director of the Wisconsin Improvement Program

Lester 5. Golub

Lecturer in Curviculum and Instruction and in English

Psychology

Thomas A. Romberg Herbert J. Klausmeier

Director, R & D Center Professor of Educational

Associate Professor of Mathematics and Curriculum

Burton W. Kreitlow Professor of Educational Policy

and Extension Education

Curriculum and Instruction

Assistant Professor of Mathematics and of

Richard L. Venezky Assistant Professor of English and of Computer Sciences Studies and of Agricultural

MANAGEMENT COUNCIL

*Herbert J. Klausmeier

Director, R & D Center Acting Director, Program 1 Thomas A. Romberg

Director Programs 2 and 3 James E. Walter

Director Dissemination Section Dan G. Woolpert

Director Operations and Business

Mary R. Quilling

Director Technical Section

* COMMITTEE CHAIRMAN



STATEMENT OF FOCUS

The Wisconsin Research and Development Center for Cognitive Learning focuses on contributing to a better understanding of cognitive learning by children and youth and to the improvement of related educational practices. The strategy for research and development is comprehensive. It includes basic research to learning and about the processes of instruction, and the subsequent development of research based instructional materials, many of which are designed for use by teachers and others for use by students. These materials are tested and refined in school settings. Throughout these operations behavioral scientists, curriculum experts, academic scholars, and school people interact, insuring that the results of Center activities are based soundly on knowledge of subject matter and cognitive learning and that they are applied to the improvement of educational practice.

This Technical Report is from Phase 2 of the Project on Prototypic Instructional Systems in Elementary Mathmatics in Program 2. General objectives of the Program are to establish rationale and strategy for developing instructional systems, to identify sequences of concepts and cognitive skills, to develop assessment procedures for those concepts and skills, to identify or develop instructional materials associated with the concepts and cognitive skills, and to generate new knowledge about instructional procedures. Contributing to the Program objectives, the Mathematics Project, Phase 1, is developing and testing a televised course in arithmetic for Grades 1-6 which provides not only a complete program of instruction for the pupils but also inservice training for teachers. Phase 2 has a long-term goal of providing an individually guided instructional program in elementary mathematics. Preliminary activities include identifying instructional objectives, student activities, teacher activities materials, and assessment procedures for integration into a total mathematics curriculum. The third phase focuses on the development of a computer system for managing individually guided instruction in mathematics and on a later extension of the system's applicability.



ACKNOWLEDGEMENTS

Many people have contributed to the completion of this study. However, I would like to thank in particular Dr. Thomas A. Romberg for the guidance and knowledge he imparted to me during my three years of graduate study. Appreciation is also extended to the other members of the reading committee, Drs. John G. Harvey and Robert E. Davidson for their help and comments concerning the study.

The author is deeply grateful to the staff of the Research and Development Center for their support in providing a teacher, technical advice, and clerical help. The author is particularly grateful to Mrs. Carolyn Gornowicz who taught the unit.

My deepest appreciation is expressed to my wife, Gloria, for her typing of rough drafts, proofreading, etc; but more importantly for her understanding and encouragement.



TABLE OF CONTENTS

ACKNOWLEDGEMENTS		FP	LG1
LIST OF TABLES	ACKNOWLE	EDGEMENTS	iv
CHAPTER I. THE PROBLEM: CAN A UNIT IN PROBABILITY BE CONSTPUCTED AND SUCCESSFULLY TAUGHT TO SIXTH GRADE STUDENTS Rationale Recommended Content Recommended Approach Existing Materials in Probability and Statistics School Mathematics Study Group AAAS Singer Scott Foresman Other Publishers Summary of Status Studies and Related Experiments Summary of Curriculum Experiments Summary of Recommendations, Existing Materials, and Research As They Relate to This Study II. DEVELOPMENT OF THE INSTRUCTIONAL PROGRAM Mathematical Analysis Content Outline Definitions Behavioral Objectives and Task Analysis Action Words Task Analysis Behavioral Objectives Learning Hierarchies Instructional Analysis Pilot Study Description of Intended Lessons Summary of Lessons Mastery Learning Criteria Formative Evaluation Test 70	LIST OF	FIGURES	vi
THE PROBLEM: CAN A UNIT IN PROBABILITY BE CONSTRUCTED AND SUCCESSFULLY TAUGHT TO SIXTH GRADE STUDENTS	LIST OF	TABLES	/ i j
I. THE PROBLEM: CAN A UNIT IN PROBABILITY BE CONSTBUCTED AND SUCCESSFULLY TAUGHT TO SIXTH GRADE STUDENTS Rationale	ABSTRACT	T	x
Rationale			
Rationale Recommended Content Recommended Approach Recommended Approach Existing Materials in Probability and Statistics School Mathematics Study Group AAAS 1 Singer 12 Scott Foresman 12 Other Publishers 16 Summary of Status Studies and Related Experiments 17 Summary of Curriculum Experiments 22 Summary of Recommendations, Existing Materials, and Research As They Relate to This Study 26 II. DEVELOPMENT OF THE INSTRUCTIONAL PROGRAM 31 Mathematical Analysis 32 Content Outline 34 Definitions 36 Behavioral Objectives and Task Analysis 40 Action Words 41 Task Analysis 42 Behavioral Objectives 42 Learning Hierarchies 45 Instructional Analysis 49 Pilot Study 49 Description of Intended Lessons 57 Summary of Lessons 60 Mastery Learning 63 Criteria 67 Formative Evaluation 69	I.		
Recommended Approach Recommended Approach Existing Materials in Probability and Statistics School Mathematics Study Group AAAS AAAS Singer Scott Foresman Other Publishers Summary of Status Studies and Related Experiments Summary of Curriculum Experiments Summary of Recommendations, Existing Materials, and Research As They Relate to This Study II. DEVELOPMENT OF THE INSTRUCTIONAL PROGRAM Mathematical Analysis Content Outline Definitions Behavioral Objectives and Task Analysis Action Words Task Analysis Behavioral Objectives Learning Hierarchies Instructional Analysis Pilot Study Description of Intended Lessons Summary of Lessons Mastery Learning Criteria Formative Evaluation Test Tomps Task Probability and Statistics Experiments Study Group AAAAS 12 81 82 83 84 84 85 86 86 87 88 88 88 89 80 80 80 80 80 80		AND SUCCESSFULLY TAUGHT TO SIXTH GRADE STUDENTS	Ī
Recommended Approach Recommended Approach Existing Materials in Probability and Statistics School Mathematics Study Group AAAS AAAS Singer Scott Foresman Other Publishers Summary of Status Studies and Related Experiments Summary of Curriculum Experiments Summary of Recommendations, Existing Materials, and Research As They Relate to This Study II. DEVELOPMENT OF THE INSTRUCTIONAL PROGRAM Mathematical Analysis Content Outline Definitions Behavioral Objectives and Task Analysis Action Words Task Analysis Behavioral Objectives Learning Hierarchies Instructional Analysis Pilot Study Description of Intended Lessons Summary of Lessons Mastery Learning Criteria Formative Evaluation Test Tomps Task Probability and Statistics Experiments Study Group AAAAS 12 81 82 83 84 84 85 86 86 87 88 88 88 89 80 80 80 80 80 80		Rationale	2
Recommended Approach		Recommended Content	(
Existing Materials in Probability and Statistics School Mathematics Study Group AAAS		Recommended Approach	7
School Mathematics Study Group AAAS 1. Singer 1. Singer 1. Scott Foresman 1. Other Publishers 1. Other Publishers 1. Summary of Status Studies and Related Experiments 1. Summary of Curriculum Experiments 2. Summary of Recommendations, Existing Materials, and Research As They Relate to This Study 2. Summary of The Instructional Program 3. Study 3.		Existing Materials in Probability and Statistics	8
AAAS Singer Scott Foresman Other Publishers Summary of Status Studies and Related Experiments Summary of Curriculum Experiments Summary of Recommendations, Existing Materials, and Research As They Relate to This Study II. DEVELOPMENT OF THE INSTRUCTIONAL PROGRAM Mathematical Analysis Content Outline Definitions Behavioral Objectives and Task Analysis Action Words Task Analysis Behavioral Objectives Learning Hierarchies Instructional Analysis Pilot Study Description of Intended Lessons Summary of Lessons Mastery Learning Criteria Formative Evaluation Test Total Test Total Total Test Tot		School Mathematics Study Group	Č
Scott Foresman		AAAS	1.1
Scott Foresman 15	•	Singer	
Other Publishers			
Summary of Status Studies and Related Experiments		Other Publishers	
Summary of Curriculum Experiments 22 Summary of Recommendations, Existing Materials, and Research As They Relate to This Study 28		Summary of Status Studies and Related Experiments	
Summary of Recommendations, Existing Materials, and Research As They Relate to This Study 28 II. DEVELOPMENT OF THE INSTRUCTIONAL PROGRAM 31 Mathematical Analysis 32 Content Outline 34 Definitions 36 Behavioral Objectives and Task Analysis 40 Action Words 41 Task Analysis 42 Behavioral Objectives 42 Learning Hierarchies 45 Instructional Analysis 49 Pilot Study 49 Description of Intended Lessons 57 Summary of Lessons 60 Mastery Learning 63 Criteria 67 Formative Evaluation 69 Test 70		Summary of Curriculum Experiments	
Research As They Relate to This Study 28 II. DEVELOPMENT OF THE INSTRUCTIONAL PROGRAM 31 Mathematical Analysis 32 Content Outline 34 Definitions 36 Behavioral Objectives and Task Analysis 40 Action Words 41 Task Analysis 42 Behavioral Objectives 42 Learning Hierarchies 45 Instructional Analysis 49 Pilot Study 49 Description of Intended Lessons 57 Summary of Lessons 60 Mastery Learning 63 Criteria 67 Formative Evaluation 69 Test 70		Summary of Recommendations Existing Materials and	22
Mathematical Analysis 32 Content Outline 34 Definitions 36 Behavioral Objectives and Task Analysis 40 Action Words 41 Task Analysis 42 Behavioral Objectives 42 Learning Hierarchies 45 Instructional Analysis 49 Pilot Study 49 Description of Intended Lessons 57 Summary of Lessons 60 Mastery Learning 63 Criteria 67 Formative Evaluation 69 Test 70		Research As They Relate to This Study	28
Mathematical Analysis 32 Content Outline 34 Definitions 36 Behavioral Objectives and Task Analysis 40 Action Words 41 Task Analysis 42 Behavioral Objectives 42 Learning Hierarchies 45 Instructional Analysis 49 Pilot Study 49 Description of Intended Lessons 57 Summary of Lessons 60 Mastery Learning 63 Criteria 67 Formative Evaluation 69 Test 70	II.	DEVELOPMENT OF THE INSTRUCTIONAL PROGRAM	31
Content Outline 34 Definitions 36 Behavioral Objectives and Task Analysis 40 Action Words 41 Task Analysis 42 Behavioral Objectives 42 Learning Hierarchies 45 Instructional Analysis 49 Pilot Study 49 Description of Intended Lessons 57 Summary of Lessons 60 Mastery Learning 63 Criteria 67 Formative Evaluation 69 Test 70			
Content Outline 34 Definitions 36 Behavioral Objectives and Task Analysis 40 Action Words 41 Task Analysis 42 Behavioral Objectives 42 Learning Hierarchies 45 Instructional Analysis 49 Pilot Study 49 Description of Intended Lessons 57 Summary of Lessons 60 Mastery Learning 63 Criteria 67 Formative Evaluation 69 Test 70		Mathematical Analysis	32
Behavioral Objectives and Task Analysis 40 Action Words 41 Task Analysis 42 Behavioral Objectives 42 Learning Hierarchies 45 Instructional Analysis 49 Pilot Study 49 Description of Intended Lessons 57 Summary of Lessons 60 Mastery Learning 63 Criteria 67 Formative Evaluation 69 Test 70		Content Outline	34
Action Words		Definitions	36
Action Words		Behavioral Objectives and Task Analysis	40
Task Analysis 42 Behavioral Objectives 42 Learning Hierarchies 45 Instructional Analysis 49 Pilot Study 49 Description of Intended Lessons 57 Summary of Lessons 60 Mastery Learning 63 Criteria 67 Formative Evaluation 69 Test 70		Action Words	41
Behavioral Objectives 42 Learning Hierarchies 45 Instructional Analysis 49 Pilot Study 49 Description of Intended Lessons 57 Summary of Lessons 60 Mastery Learning 63 Criteria 67 Formative Evaluation 69 Test 70		Task Analysis	42
Learning Hierarchies 45 Instructional Analysis 49 Pilot Study 49 Description of Intended Lessons 57 Summary of Lessons 60 Mastery Learning 63 Criteria 67 Formative Evaluation 69 Test 70		Behavioral Objectives	42
Instructional Analysis 49 Pilot Study 49 Description of Intended Lessons 57 Summary of Lessons 60 Mastery Learning 63 Criteria 67 Formative Evaluation 69 Test 70		Learning Hierarchies	45
Pilot Study 49 Description of Intended Lessons 57 Summary of Lessons 60 Mastery Learning 63 Criteria 67 Formative Evaluation 69 Test 70		Instructional Analysis	
Description of Intended Lessons 57 Summary of Lessons 60 Mastery Learning 63 Criteria 67 Formative Evaluation 69 Test 70		Pilot Study	
Summary of Lessons 60 Mastery Learning 63 Criteria 67 Formative Evaluation 69 Test 70		Description of Intended Lessons	
Mastery Learning 63 Criteria 67 Formative Evaluation 69 Test 70			
Criteria		Mastery Learning	
Formative Evaluation		Criteria	
Test		Formative Evaluation	
Summary of Chapter			
		Summary of Chapter	71



TABLE OF CONTENTS (CONTINUED)

CHAPTER							PAGE
III.	THE DESIGN AND CONDUCT OF THE STUDY	•	•	•	•	•	73
	Instructional System				•		73
	Input						74
	Population			•			74
	The Sample					•	75
	Resources		·	•	•	•	77
	Teaching Staff	•	•	•	•	•	77
	Auxilary Staff	•	•	•	•	•	77 78
	Classroom Facilities and Equipment .	•	•	•	•	•	
	Instructional Program and Feedback	•	•	•	•	•	78 70
	Classroom Organization	•	•	•	•	•	79
	Lessons	•	•	•	•	•	79
	Evaluation	•	•	•	•	•	80
	Evaluation	•	•	•	•	•	80
	Mastery Learning	•	•	•	•	•	81
	Output	•	•	•	•	•	82
	Conduct of Study	•	•	•	•	•	82
	Description of the Journal	•	•	•	•	•	82
	Description of the Study	•	•	•	•		83
	Pretest						83
	Actual Instruction and Evaluation	•	•	•	•	•	87
IV.	RESULTS	•	•	•	•		93
	Validity						· .
	Validity	•	•	•	•	•	94
	Reliability	•	•	•	•	•	94
	Overall Results	•	•	•	•	•	94
	Behavioral Objectives	•	•	•	•	•	96
	One-Dimensional and Two-Dimensional Results	•	•	•	•	•	106
	Learning Hierarchy	•	•	•	•	•	106
V .	SUMMARY, CONCLUSIONS, AND RECOMMENDATIONS						113
	Summary	•	•	•	•	•	113
	Purpose	•	•	•	•	•	113
	Method	•	•	•	•	•	
	Conclusions	•	•	•	•	•	113
	Conclusions: Formative Study	•	•	•	•	•	114
	Objectives Not Ashioved	•	•	•	•	•	115
	Objectives Not Achieved One-Dimensional and Two-Dimensional Sa	•	•		•	•	115
	Spaces	ımţ	эте	2			101
	Alternative Hypotheses	•	•	•	•	•	121
	Testing of Tearning Winnership.	•	•	•	•	•	121
	Testing of Learning Hierarchies Major Objectives Not Measured by Test	•	•	•	•	•	123
	Quizzes	υĽ	•				125
		•	•	•	•	•	エムノ



TABLE OF CONTENTS (CONTINUED)

CHAPTER		PAGE
	Conclusions: Developmental Procedures and	
	Materials	126
	Major Suggested Changes	127
	Mastery Learning	129
	Criteria	129
	Limitations of the Study	130
	Recommendations As to the Use of the Materials	
	Recommendations for Further Study	131
APPENDIX A.	JOURNAL OF STUDY (INCLUDING LESSON PLANS, EXERCISES, QUIZZES AND COMMENTS)	133
APPENDIX B.	TESTING INSTRUMENT USED FOR PRETESTING AND POSTTESTING	361
APPENDIX C.	TABLES PRESENTING DATA FROM THE FORMATIVE EVALUATION	202
	HVALUATION	383
APPENDIX D.	BACKGROUND DATA OF STUDENTS	403
BIBLIOGRAPH	IY	405



LIST OF FIGURES

FIGURE		P	AGE
1	Steps in Developing an Instructional System	•	33
2	Tree Diagram for Spinner	•	39
3	Task Analysis of Probability And Statistics Concept For the Elementary School		43 A
4	Learning Hierarchy 1		46
5	Learning Hierarchy 2	•	46
6	A Sample Problem in Deciding Between Two Boxes		47
7	Learning Hierarchy 3		48
8	Instruction Plan for the Probability UnitAnticipated Number of Days (20-22) 50 Minutes Per Day		58
9	The Basic Elements of an Instructional System		74
10	Sequence of Lessons, Exercises and Quizzes		84
11	Percentage Graph of Behavioral Objectives as Measured By the Pretest and Posttest		102
12	Percentage Graph of Behavioral Objectives Concerned With Both 1-D and 2-D Problems as Measured by the Pretest and Posttest		105
13	Picture of a Typical Learning Hierarchy		106
14	Learning Hierarchy Components		107
15	Items Designed to Measure Behavioral Objective 2		117
16	Item (13, 1) Used to Measure Objective 8		119
17	Item (14, 2) Used to Measure Objective 11		119



LIST OF TABLES

F ABLE	P.	AGE
1	Posttest Results of Pilot Study	54
2	Iowa Test Scores of the 25 Subjects in the Study	76
3	Summary of Quiz Results Measuring Any of the Major Behavioral Objectives	91
4	Overall Results of the Pretest and Posttest	9 :
5	Item Percentages of the Pretest and Posttest	99
6	Level of Achievement of the Fourteen Behavioral Objectives	101
7	Summary Table of Behavioral Objectives (Percentages of of Correct Responses)	103
8	Partitioning of Students in Learning Hierarchy 1 By Objectives: Test Criterion90%	109
9	Partitioning of Students in Learning Hierarchy 1 Practical Test Criterion	110
10	Partitioning of Students in Learning Hierarchy 2 Test Criterion 90%	111
11	Partitioning of Students in Learning Hierarchy 2 Practical Test Criterion	11:
12	Results in Criteria Form for Objectives Not Achieved	116
13	Behavioral Objective 2	116
14	Ratios for Testing Hierarchy 1 Using Two Criteria	123
15	Ratios for Testing Hierarchy 2 Using Two Criteria	124



ABSTRACT

From a content outline and a task analysis the behavioral objectives for a unit of instruction in probability and statistics for sixth-grade students and the order in which objectives would be taught were determined. An instructional analysis of the unit was undertaken to select or develop materials and procedures for teaching the unit.

Data from a pilot study conducted in the fall of 1969 were used to identify a set of nine lessons that could be formatively evaluated to test the feasibility of the instructional analysis. The lessons were used to teach a class of 25 sixth-grade students of average to above average ability. The topics developed through experiments, games and exercises were subjective probability notions, empirical probability, counting techniques, a priori probability including simple and compound events, and comparison of two events using probability.

On the basis of the overall pretest and posttest the instructional treatment was generally successful. The pretest percentage was 37.9% and the posttest percentage was 92.8% with all 72 items successful for 11 of the 14 measured objectives. Instruction was unsuccessful in getting students to specify the estimated probability; number the outcomes of an event; and estimate the probability successful for these three objectives because of a lack of stress and practice. Two learning hierarchies were also tested. One hierarchy was validated and the other was not. The results of the study support the feasibility of teaching most of the included topics in probability and statistics to average and above average sixth-grade students given high quality of teaching. lends support to the use of the systems developmental model employed in this study for developing curriculum materials for the schools, especially when used in conjuction with Bloom's "Mastery Learning" techniques.



APPENDIX B

TESTING INSTRUMENT USED FOR PRETESTING AND POSTTESTING



Name					

Instructions

Place your name in the blank at the left.

(Do not turn this page until you are told)

The questions you are about to answer were written to find out how much you know about a certain branch of mathematics that deals with "luck" or "probability". Read each question very carefully and write your answers in the answer blanks provided. If the question is a multiple choice question place the letter you think is correct in the blank provided.

There are different kinds of questions. Some questions ask, "what is the probability of ...". Others ask you to tell "how many" or "which game gives you the best chance of winning". Be sure you answer each question in the proper way. Read carefully.

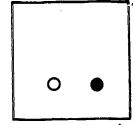
Since you have not studied this topic before, there will be questions for which you do not know the answers. Leave such questions blank. Do not guess.

It is assumed that each game or activity is to be played fairly.

You may take as much time as you need to do the test. Work carefully. You may use the blank space by a question to do your scratch work.



For problems (1 - 8), a marble is picked from the box below one or more times. After a marble is picked the color is recorded and the marble is returned to the box. Classify the statements about chance as being certain to happen, uncertain as to whether it could happen, or impossible to happen. Place the letter that indicates your choice in the blank.



- 1. The chances of getting a black or white marble in picking from the box are (a) certain (b) uncertain (c) impossible.
- 2. The chances of getting a striped marble in picking from the box are (a) certain (b) uncertain (c) impossible.
- 3. The chances of getting 50 black marbles in picking from a box 50 times are (a) certain (b) uncertain (c) impossible.
- 4. The number of black in picking 100 times from the box may be
 0 or 100 or anything in between is (a) certain (b) uncertain
 (c) impossible.



The following statements are true or false. If you think a statement is true, put a T in the blank after the statement. If you think the statement is <u>not true</u>, put an F in the blank. The problems pertain to the picture at the right.

0 0

- _____ 5. It is possible to pick 200 times without getting a single black marble.
- 6. If we pick a marble 1000 times it is likely that we will get between 400 and 600 blacks.
- 7. You have picked from the box 5 times and have gotten 5 black marbles. It is more likely that the next pick will be white than black.
- 8. You have picked from the box 30 times and have gotten 30 white marbles in a row. You are almost certain to get a black marble in the next pick from the box.



Multiple Choice

- 1. If you spin the fair spinner at the right 10 times and get 10 red, the chances of getting white on the 11th spin are
 - (a) almost certain
 - (b) 1/2
 - (c) certain
 - (d) none of the above
- 2. You draw a marble without looking, from the box below
 20 times and get 20 black marbles. Each time you pick a marble
 you put it back. The chances of getting a black marble on the
 - (a) impossible
 - (b) almost impossible
 - (c) 1/3
 - (d) none of the above



R

W



Identify whether the following fractions are equal or if one is larger than the other.

- 1. 2/6, 1/3

 - (a) 2/6 = 1/3 (b) 2/6 is greater than 1/3
 - (c) 1/3 is greater than 2/6
- _____ 2. 1/2, 1/3

 - (a) 1/2 = 1/3 (b) 1/2 is greater than 1/3
 - (c) 1/3 is greater than 1/2
- 3. 2/8, 3/9

 - (a) 2/8 = 3/9 (b) 2/8 is greater than 3/9
 - (c) 3/9 is greater than 2/8
- ____ 4. 1/2, 3/6

 - (a) 1/2 = 3/6 (b) 1/2 is greater than 3/6
 - (c) 3/6 is greater than 1/2
- ____ 5. 1/5, 2/10

 - (a) 1/5 = 2/10 (b) 1/5 is greater than 2/10
 - (c) 2/10 is greater than 1/5
- ____ 6. 2/10, 1/8

 - (a) 2/10 = 1/8 (b) 2/10 is greater than 1/8
 - (c) 1/8 is greater than 2/10
- 7. 2/3, 2/4

 - (a) 2/3 = 2/4 (b) 2/3 is greater than 2/4
 - (c) 2/4 is greater than 2/3



- 8. 1/4, 3/12

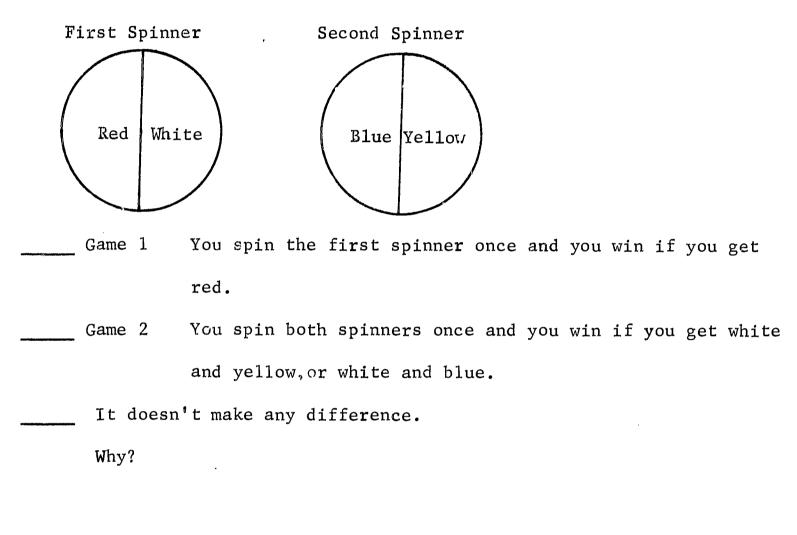
 - (a) 1/4 = 3/12 (b) 1/4 is greater than 3/12
 - (c) 3/12 is greater than 1/4
- 9. 3/8, 2/5

 - (a) 3/8 = 2/5 (b) 3/8 is greater than 2/5
 - (c) 2/5 is greater than 3/8
- 10. 1/4, 7/16

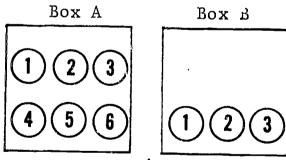
 - (a) 1/4 = 7/16 (b) 1/4 is greater than 7/16
 - (c) 7/16 is greater than 1/4.

The following set of problems ask you to choose the game which gives you the best chance of winning. If the chances are the same you are to identify that it doesn't make any difference. Place an X in the blank to the left of the choice which you think is correct. Give a short explanation as to why you gave the answer you did.

1. Which game gives you the best chance of winning or doesn't it make any difference?



2. Which game gives you the best chance of winning or doesn't it make any difference?

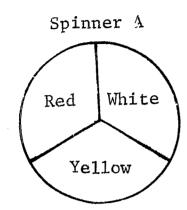


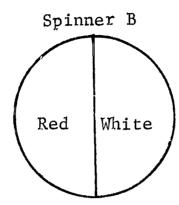
- Game 1 You pick a chip from Box A and you win if you pick the chip with "2" on it.
- Game 2 You pick twice from Box B (without putting the first chip back). You win if you get a "1" on the first pick and a "2" on the second pick.
- It doesn't make any difference.

Which game gives you the best chance of winning or doesn't it make any difference? Box A Box B You pick a chip from Box A and you win if you pick the Game 1 chip with "3" on it. You pick one chip from Box A and one chip from Box B. Game 2 You win if you get a "3" from Box A and a "2" from Box B. It doesn't make any difference. Why? Which game gives you the best chance of winning or doesn't it make any difference? Box A Box B You pick a chip from Box A and you win if you pick the Game 1 chip with "1" on it. Game 2 You pick one chip from Box A and one chip from Box B and find the sum of the numbers on the chips. You win if the sum is It doesn't make any difference. Why?



5. Which game gives you the best chance of winning or doesn't it make any difference?





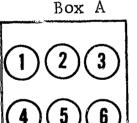
Game 1 You spin Spinner A once and you win if you get white,

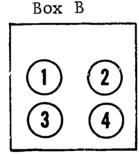
Game 2 You spin Spinner B twice. You win if you get Red on the first spin and White on the second spin.

____ It doesn't make any difference.

Why?

6. Which game gives you the best chance of winning or doesn't it make any difference?





Game 1 You

You pick a chip from Box A and you win if you pick the chip with "2" on it.

Game 2 You pick twice from Box B (without putting the first chip you pick back). You win if you pick a "2" first and a "4" on the second pick.

It doesn't make any difference.

Why?

7.	Which game	gives you the best chance of winning or doesn't it
	make any di	fference?
	Вож А	Вож В
	(1) (2) (3) (4)	1 2 3 4
	Game 1	You pick one chip from Box A and you win if you get a
		chip with a "4" on it.
	Game 2	You pick one chip from Box A and one from Box B and find
		the sum of the numbers on the chips. You win if you get
		a sum of $\frac{4}{}$ or $\frac{5}{}$.
	It doesn	't make any difference.
	Why?	



The following boxes contain black and white marbles. To play this game you pick a marble from one of the two boxes. You win if you choose a black marble.

If you can play this game only once, do you have a better chance of winning if you pick from Box A or Box B, or doesn't it make any difference?

For each question, place an "X" in the blank at the right that shows your choice.

1.	Box A	Box B		
	0	•00	make paper part (SE) in the first of the following	Box A
	• 0	000		Box B
				It doesn't make any difference
2.	Box A	Box B		
		•		Box A
		00		Box B
	 			It doesn't make any difference
3.	Box A_	Box B		
	0000	0000		Box A
	●000	0000	Maria de Carlos	Box B
				It doesn't make any difference
4.	Box A	Box B		
		•00		Box A
	0 •	000		Box B
		ļ		It doesn't make any difference
5.	Box A	Box B		D A
		000		Box A
	• 0	000		Box B
	1			It doesn't make any



6.	Box A	Вох В			
				Box A	
•	0 •	• 0		Box B	
			encological processor Promone	It doesn't make an difference	y
7.	Box A	Box B	***************************************	Вож А	
	00	00		Вох В	
		0000	array person demandrate reconstitute	It doesn't make an	137
		•	Annual and Annual Annual and Annual and Annual and Annual and Annual and Annual and Annual Annual Annual Annua	difference	·y
8.	Вох А	Box B			
	0000	0000		Box A	
	0000	0000	•	Box B	
		Annual and State of the state o	Marine de la constitución de la	It doesn't make ardifference	y
9.	Box A	Box B			
	●000	• •		Box A	
	000	000	Commission of the State of the	Box B	
	<u></u>	<u> </u>		It doesn't make ar difference	ıy
10.	Box A	Box B			
	•	0 • •		Box A	
	0 •	• • •		Box B	
	les grantes de l'estre	<u></u>	And property against the of Michigan Street, and	It doesn't make ar difference	ıy
11.	Box A	Box B			
	• 0			Box A	
	• •		**************************************	Box B	
			fat designifullsyken die Felle begengs	It doesn't make ar	ıy



For the following problems a marble is drawn without looking from a bag containing 4 white marbles and 1 red marble.

1. How many possible outcomes are there?

2. What is the probability of getting a red marble?

3. What is the probability of getting a white marble?

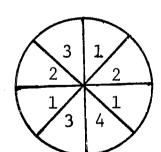
4. What is the probability of getting a red or white marble?

5. What is the probability of getting a green marble?

R 7

For the following problems you spin the spinner below one time.

- 1. How many possible outcomes are there?
- 2. How many ways can you get a "1"?
- 3. What is the probability of getting a "1"?
- 4. What is the probability of getting a "4"?





For the following problem you spin the spinner at the right two times.

1. How many possible outcomes are there?

2. How many ways can one get white on the first spin and white on the second spin?

3. What is the probability of getting red on the first spin and red on the second spin?

4. What is the probability of getting red on the first spin and either color on the second spin?



			Box A	Вох В
	numl	the following problems you pick a bered chip without looking from Box and one from Box B.	3	3 4
	1.	How many possible outcomes are there?		
	2.	How many ways can one get a sum of '4" the chips are added together?	when the two	numbers on
	3.	What is the probability of getting "1" Box B?	from Box A a	and "1" from
	4.	What is the probability of getting an equal to 5?	outcome whose	sum is
***************************************	5.	What is the probability of getting an equal to 8?	outcome whose	sum is



For the following problems you spin the spinner at the right two times.

1. How many possible outcomes are there?

2. What is the probability of getting a "2" on the first spin and a "4" on the second spin?

3. What is the probability of getting an outcome whose sum is equal to 2?

4. What is the probability of getting an outcome whose sum is equal to 6?

5. What is the probability of getting an outcome whose sum is less than 10?



For the following problem a die is thrown which turns up is recorded.

1. How many possible outcomes are there?

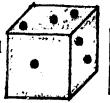
2. How many ways can one get a "3" or a "5"?

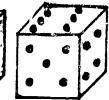
3. What is the probability of getting a "2"?

4. What is the probability of getting a "3" or a "5"?



For the following problem, two dice are thrown, one red and one white. The sum of the faces turning up is recorded.



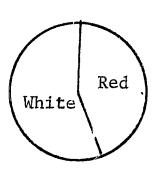


- 1. How many ways can all the sums be gotten?
- 2. How many ways can one get the sum 2 or 3?
- $\underline{}$ 3. What is the probability of getting the sum $\underline{12}$?
- 4. What is the probability of getting the sum 11?
- 5. What is the probability of getting a sum of 2 or 3?



380

1. In 6000 spins of the spinner at the right Bob gets 2653 reds. What is the estimated probability of getting a red on the next spin?





1. Bob tossed a thumbtack 9,000 times with the following results:

Which of the following statements could Bob make?

- a. The chances of the thumbtack pointing down is about 1/2.
- b. The chances of the thumbtack pointing down is about 1/3.
- c. The chances of the thumbtack pointing down is exactly 2997/6003.
- d. The chances of the thumbtack pointing down is exactly 2997/9000.
- e. Bob can make no statement at all about the chances of the thumbtack pointing down.



APPENDIX C

TABLES PRESENTING DATA FROM THE FORMATIVE EVALUATION

Tables 16 through 29 present the pretest and posttest data for each of the measured behavioral objectives. The first column of each table lists as an ordered pair the part and the item number for the test (see). For example (1,5) means that the item is Item 5 in Part I of the test in Appendix B. (E.g. (1, 5) is

"5. It is possible to pick 200 times without getting a single black marble."

The number of correct responses on item (1, 5) for the pretest was 4 (out of 25) and for the posttest was 22 (out of 25).

The total number of correct responses for the items is listed under "Total." With regard to items measuring a behavioral objective in a one dimensional (1D) and a two dimensional sample space (2D), the data is presented separately under the headings "1D" and "2D." The "Total" in this case presents the sum of the correct responses in "1D" and "2D" separately while the "Grand Total" combines the results' of "1D" and "2D" columns together.

One should keep in mind that the total number of possible correct responses for item is 25, the number of children in the study.



TABLE 16

BEHAVIORAL OBJECTIVE 1 -- DISTINGUISH WHETHER AN EVENT IS AN INSTANCE OF CERTAINTY, UNCERTAINTY, OR IMPOSSIBILITY. (5 ITEMS)

Item N	Number	No. of correct	No. of Correct
Part	Item	responses (Pretest)	responses (Posttest)
(1,	1)	18	25
(1,	2)	23	25
(1,	3)	18	23
(1,	4)	15	24
(1,	5)	14	22
Tota1		88	119

TABLE 17

BEHAVIORAL OBJECTIVE 2 -- COUNT THE NUMBER OF OUTCOMES OF AN EVENT (5 ITEMS)

Item Number	No. of (Correct	No. of Correct			
	respo		responses			
	(Pret	test)	(Fostt	est)		
Part Item	1D	2D	1D	2D		
(7, 2)	21		25			
(8, 2)		4		16		
(9, 2)		6		22		
(11, 2)	7		17			
(12, 2)		1		19		
Total	28	11	42	57		
Grand Total 1D and 2D	3	9	9:	9		



BEHAVIORAL OBJECTIVE 3 -- COUNT THE NUMBER OF POSSIBLE OUTCOMES OF A SAMPLE SPACE (7 ITEMS)

Item Number		respo	No. of Correct responses (Pret e st)		No. of Correct responses (Posttest)	
<u>Part</u>	Item	1D	2D	1D	2D	
(6,	1)	11		24		
(8,	1)		1		25	
(10,	1)		o		23	
(12,	1)		0		22	
(7,	1)	12		25		
(9,	1)		0		23	
(11,	1)	21		23		
Total		44	1	72	93	
Grand 1D and		45	5	16	55	



TABLE 19

BEHAVIORAL OBJECTIVE 4a -- SPECIFY THE PROBABILITY OF A SIMPLE EVENT (8 ITEMS)

Item Number	No. of C respo (Pret	nses	No. of or responding the contract of the contr	nses
Part Item	1D	2D	1D	2D
(6, 2)	7		25	
(8, 3)		0		25
(10, 2)		o		25
(10, 3)		0		25
(12, 3)		0		25
(7, 4)	8		25	
(9, 3)		0		25
(11, 3)	6		24	
Total	21	0	74	125
Grand Total			199)



TABLE 20 - BEHAVIORAL OBJECTIVE 4b -- SPECIFY THE PROBABILITY OF A COMPOUND EVENT (8 ITEMS)

	No. of	Correct	No. of C	Correct
	respon	nses	respon	ises
Item Number	(Prete	est)	(Postte	est)
Part Item	1 D	2D	1D	2D
(6, 3)	6		25	
(8, 4)		2		23
(10, 4)		1		25
(12, 4)		0		24
(12, 5)		0		25
(7, 3)	8		25	
(9, 4)		0		21
(11, 4)	4		23	
Tota1	18	3	73	118
Grand Total 1	D and 2D 2	1	191	

TABLE 21

BEHAVIORAL OBJECTIVE 4c -- SPECIFY THE PROBABILITY OF A CERTAIN EVENT (2 ITEMS)

Item Number	No. of (Respo	onse	No. of C Respo (Postt	nse
Part Item	1D	2D	1 D	2D
(6, 4)	3		24	
(10, 5)		5		23
Total	3	5	24	23
Grand Total 1D and	1 2D 8	3	47	



TABLE 22

BEHAVIORAL OBJECTIVE 4d -- SPECIFY THE PROBABILITY OF THE IMPOSSIBLE EVENT (2 ITEMS)

Item Number	- 1	Correct onses test)	res	Correct ponses ttest)
Part Item	1D	2D	1.D	2D
(6, 5)	12		25	
(9, 5)		5		24
Total	12	5	25	24
Grand Total (1D and 2D	1	7		49

TABLE 23

BEHAVIORAL OBJECTIVE 5 -- SPECIFY THE ORDER OF TWO FRACTIONS BETWEEN O AND 1 (10 ITEMS)

Item Number Part Item	No. of Correct Responses (Pretest)	No. of Correct Responses (Posttest)
(3, 1)	24	25
(3, 2)	22	25
(3, 3)	16	24
(3, 4)	24	25
(3, 5)	24	25
(3, 6)	18	23
(3, 7)	17	24
(3, 8)	22	25
(3, 9)	17	23
(3, 10)	13	21
Tota1	197	240



BEHAVIORAL OBJECTIVE 6 -- IDENTIFY THE MOST LIKELY EVENT OF TWO UNEQUALLY LIKELY EVENTS (10 ITEMS)

		No. o	f correct	No. of correct	
		res	pouses	rep	onses
Item N	umber	(Pr	etest)	(Pos	ttest)
Part	Item	1D	1D and 2D	1D	1D and 2D
1410					
(4,	3)		10		24
(4,	5)		4		23
(4,	6)		2		23
(4,	7)		13		20
(5,	2)	15		24	
(5,	3)	18		25	
(5,	5)	17	·	25	
` ,	ŕ				
(5,	6)	15		24	
(5,	8)	13		25	
(5,	9)	13		25	
Total		91	29	148	90
Grand	Total				
	lus 1D and	2D) 1	20	4 2	238

TABLE 25

BEHAVIORAL OBJECTIVE 7 -- IDENTIFY TWO UNEQUALLY LIKELY EVENTS AS BEING EQUALLY LIKELY (8 ITEMS)

;		f correct	•	correct
	responses			onses
Item Number	•	etest)	(Post	
Part Item	1D	1D and 2D	1D	1D and 2D
(4, 1)		9		23
(4, 2)		7		22
(4, 4)		4		23
(5, 1)	8		23	
(5, 4)	8		25	
(5, 7)	13		24	
(5, 10)	7	; ;	23	
(5, 11)	8		23	
Total Number of Correct Respons	es 44	20	118	68
Grand Total (1D plus 1D and	2D)	64		186

TABLE 26

BEHAVIORAL OBJECTIVE 8 -- SPECIFY THE ESTIMATED PROBABILITY OF AN EVENT, GIVEN THE DATA FROM AN EXPERIMENT (1 ITEM)

Item Numb	er	No. of correct responses (Pretest)	No. of correct responses (Posttest)
13,	1	2	13



TABLE 27

BEHAVIORAL OBJECTIVE 9 -- IDENTIFY THE LIKELY BOUNDS ON THE FREQUENCY
OF AN OUTCOME OF AN EXPERIMENT PERFORMED
N TIMES (1 ITEM)

	No. of correct	No. of correct
Item Number	responses	responses
Part Item	(Pretest)	(Posttest)
(1, 6)	10	25
· /		

TABLE 28

BEHAVIORAL OBJECTIVE 10 -- IDENTIFY AN INSTANCE OF THE LAW OF AVERAGES (4 ITEMS)

Item Number Part Item	No. of correct responses (Pretest)	No. of correct responses (Posttest)
(1, 7)	16	22
(1, 8)	1 5	22
(2, 1)	10	23
(2, 2)	8	25
Total Number of correct responses	49	92

TABLE 29

BEHAVIORAL OBJECTIVE 11 -- IDENTIFY AN ESTIMATE OF THE PROBABILITY GIVEN A SET OF DATA FROM AN EXPERIMENT (1 ITEM)

	No. of correct	No. of correct
Item Number	responses	responses
Part Item	(Pretest)	(Posttest)
14, 1	1	7



Tables 30 through 43 present the break-down of the ratio of students achieving a specified test criterion level on the posttest. For example, in Table 30, 24 students out of 25 (96%) scored 80% or better (4/5 or 5/5) on the five items measuring Behavioral Objective 1.

TABLE 30

BEHAVIORAL OBJECTIVE 1 (POSTTEST)

Ratio of Children Reaching Test Criterion	Percentage of Children Reaching Test Criterion	Test Criterion (Ratio Form)	Test Criterion (Percentage Form)
20/25	80	5/5	100
24/25	96	4/5	80
25/25	100	3/5	60

TABLE 31
BEHAVIORAL OBJECTIVE 2 (POSTTEST)

Ratio of Children Reaching Test Criterion	Percentage of Children Reaching Test Criterion	Test Criterion (Ratio Form)	Test Criterion (Percentage Form)
11/25	44	5/5	100
18/25	72	4/5	80
22/25	88	3/5	60
22/25	88	2/5	40
25/25	100	1/5	20



TABLE 32
BEHAVIORAL OBJECTIVE 3 (POSTTEST)

Ratio of Children Reaching Test Criterion	Percentage of Children Reaching Test Criterion	Test Criterion (Ratio Form)	Test Criterion (Percentage Form)
18/25	72	7/7	100
22/25	88	6/7	85.7
25/25	100	5/7	71.4

TABLE 33
BEHAVIORAL OBJECTIVE 4a (POSTTEST)

Ratio of Children Reaching Test Criterion	Percentage of Children Reaching Test Criterion	Test Criterion (Ratio Form)	Test Criterion (Percentage Form)
24/25	96	8/8	100
25/25	100	7/8	87.5

TABLE 34
BEHAVIORAL OBJECTIVE 4b (POSTTEST)

Ratio of Children Reaching Test Criterion	Percentage of Children Reaching Test Criterion	Test Criterion (Ratio Form)	Test Criterion (Percent a ge Form)
18/25	72	8/8	100
23/25	88	7/8	87.5
25/25	100	6/8	75



TABLE 35

BEHAVIORAL OBJECTIVE 4c (POSTTEST)

Ratio Children Reaching Test Criterion	Percentage of Children Reaching Test Criterion	Test Criterion (Ratio Form)	Test Criterion (Percentage Form)
22/25	88	2/2	100
25/25	100	1/2	50

TABLE 36
BEHAVIORAL OBJECTIVE 4d (POSTTEST)

Ratio Children Reaching Test Criterion	Percentage of Children Reaching Test Criterion	Test Criterion (Ratio Form)	Test Criterion (Percentage Form)
24/25	96	2/2	100
25/25	100	1/2	50

TABLE 3 7

BEHAVIORAL OBJECTIVE 5 (POSTTEST)

Ratio Children Reaching Test Criterion	Percentage of Children Reaching Test Criterion	Test Criterion (Ratio Form)	Test Criterion (Percentage Form)
18/25	72	10/10	100
23/25	92	9/10	90
24/25	96	8/10	80
25/25	100	7/10	70



TABLE 38

BEHAVIORAL OBJECTIVE 6 (POSTTEST)

Ratio Children Reaching Test Criterion	Percentage of Children Reaching Test Criterion	Test Criterion (Ratio Form)	Test Criterion (Percentage Form)
16/ 25	64	10/10	100
23/25	92	9, 10	90
24/25	96	8/10	80
25/25	100	7/10	70

TABLE 39
BEHAVIORAL OBJECTIVE 7 (POSTTEST)

Ratio Children Reaching Test Criterion	Percentage of Children Reaching Test Criterion	Test Criterion (Ratio Form)	Test Criterion (Percentage Form)
15/25	60	8/8	100
23/25	92	7/8	87.5
24/25	96	6/8	75.0
25/25	100	4/8	50.0

TABLE 40
BEHAVIORAL OBJECTIVE 8 (POSTTEST)

Ratio Children Reaching Test Criterion	Percentage of Children Reaching Test Criterion	Test Criterion (Ratio Form)	Test Criterion (Percentage Form)
13/25	52	1/1	100



TABLE 41
BEHAVIORAL OBJECTIVE 9 (POSTTEST)

Ratio Children Reaching Test	Percentage of Children Reaching Test	Test: Criterion	Test Criterion (Percentage
Criterion	Criterion	(Ratio Form)	Form)
25/25	100	1/1	100

TABLE 42
BEHAVIORAL OBJECTIVE 10 (POSTTEST)

Ratio Children Reaching Test Criterion	Percentage of Children Reaching Test Criterion	Test Criterion (Ratio Form)	Test Criterion (Percentage Form)
21/25	84	4/4	100
22/25	88	3/4	75
24/25	96	2/4	50
25/25	100	1/4	25

TABLE 43
BEHAVIORAL OBJECTIVE 11 (POSTTEST)

Ratio Children Reaching Test Criterion	Percentage of Children Reaching Test Criterion	Test Criterion (Ratio Form)	Test Criterion (Percentage Form)
7/25	28	1/1	100



Tables 44 through 55 include results from the pretest, quiz(zes) and posttest for each behavioral object that was measured, both in a one dimensional and in a two dimensional sample space.

TABLE 44

BEHAVIORAL OBJECTIVE 3 (ONE DIMENSIONAL

Test	Number of Items	Ratio of Correct Responses	Percentage of Correct Responses
Pretest	3	44/75	
Quiz I	2	29/50	58.7 58.0
Quiz II	2	46/48	95.8
Posttest	3	72/75	96.0

TABLE 45
BEHAVIORAL OBJECTIVE 3 (TWO DIMENSIONAL)

Test	Number of	Ratio of	Percentage of
	items	Correct	Correct
		Responses	Responses
Pretest	4	1/100	1.0
Quiz IIB	2	37/48	77 . 1
Posttest	4	93/100	93.0

TABLE 46
BEHAVIORAL OBJECTIVE 4a (ONE DIMENSIONAL)

Test	Number of items	Ratio of Correct	Percentage Correct
	rcents	Responses	Responses
retest	3	21/75	28
Quiz I	1	24/25	96
Posttest	3	74/75	98.8



TABLE 47
BEHAVIORAL OBJECTIVE 4a (TWO DIMENSIONAL)

Test	Number of Items	Ratio of Correct	Percentage Correct
		Responses	Responses
Pretest	5	0/125	0
Quiz IIB	3	62/72	86.1
Quiz III	2	37/46	80.4
Posttest	5	125/125	100

TABLE 48
BEHAVIORAL OBJECTIVE 4b (ONE DIMENSIONAL)

Test	Number of Items	Ratio of Correct Responses	Percentage Correct Responses
Pretest	. 3	18/75	24
Quiz I	4	84/100	84.0
Quiz IIA	4	85/96	88.5
Quiz III Posttest	1 3	19/23 73/75	82.6 97.3

TABLE 49
BEHAVIORAL OBJECTIVE 4b (TWO DIMENSIONAL)

Test	Number of	Ratio of Correct	Percentage of Correct
	Items	Responses	Responses
Pretest	5	3/125	2.4
Quiz IIB	3	43/72	59.7
Quiz III	2	36/46	78.3
Posttest	5	118/125	84.4



TABLE 50

BEHAVIORAL OBJECTIVE 4c (ONE DIMENSIONAL)

Test	Number of Items	Ratio of Correct	Percentage of Correct
		Responses	Responses
Pretest	2	7/50	14.0
Quiz I	2	44/50	88.0
Quiz II (A and B)	2	47/48	97.9
Posttest	2	47/50	94.0

TABLE 51

BEHAVIORAL OBJECTIVE 4d (ONE DIMENSIONAL AND TWO DIMENSIONAL)

Test	Number of Items	Ratio of Correct Responses	Percentage of Correct Responses
Pretest	2	17/50	34.0
Quiz I	2	48/50	96.0
Quiz II (A and B)	2	47/48	97.9
Posttest	 2	49/50	98.0

TABLE 52
BEHAVIORAL OBJECTIVE 5 (ONE DIMENSIONAL)

Test	Number of Items	Ratio of Correct Responses	Percentage of Correct Responses
Pretest Exercise (71) Quiz IV Posttest	6 12 3 6	91/150 261/300 68/75 148/150	60.7 87.0 90.7 98.7



TABLE 53

BEHAVIORAL OBJECTIVE 6 (TWO DIMENSIONAL)

Test	Number of Items	Ratio of Correct Responses	Percentage of Correct Responses
Pretest	4	· 29/100	29.0
Quiz IV	4	83/100	83.0
Posttest	4	90/100	90.0

TABLE 54
BEHAVIORAL OBJECTIVE 7 (ONE DIMENSIONAL)

Test	Number of Items	Ratio of Correct Responses	Percentage of Correct Responses
Pretest	5	44/125	35.2
Exercise 7I	5	108/125	86.4
Quiz IV	2	48/50	96.0
Posttest	5	118/125	94.4

TABLE 55
BEHAVIORAL OBJECTIVE 7 (TWO DIMENSIONAL)

Test	Number of Items	Ratio of Correct Responses	Percentage of Correct Responses
Pretest	3	20/75	26.7
Quiz IV Posttest	5 3	105/125 68/75	84.0 90.7



TABLE 56

INDIVIDUAL PRETEST - POSTTEST RESULTS

(Number of Correct Responses on the 72 Item Test)

Subject (Student)	Pretest	Posttest	Subject (Student)	Pretest	Posttest
	25	69	14	28	99
2	23	7 9	15	7	57
೮	37	29	16	37	99
7	23	70	1.7	77	69
5	31	89	18	36	` L9
9	22	70	19	22	89
7	39	69	20	14	09
80	35	29	21	22	69
6	34	69	22	26	29
10	18	69	23	35	89
11	21	69	24	30	71
12	26	65	25	19	65
13	28	61			



APPENDIX D

BACKGROUND DATA OF STUDENTS



TABLE 57

STUDENT BACKGROUND DATA (IOWA TESTS, MATH GRADES, IQ SCORES)

IQ Test	фтоЭ	131	117	901	121	110	113	124*	114	112	116	124	124	123	118*	107	112	120*	120	124	901	125	111	126	117	122	6961
horndike Form A	Non- Verbal	122	113	102	128	103	111	96	117	111	117	128	120	125	111	109	121	113	116	117	104	120	119	126	109	118	ed March,
Lorge-T Level 3	Verbal	141	122	109	115	117	115	132	111	114	115	121	128	121	126	106	104	127	125	131	109	130	104	127	125	126	*Administered
Math Grade	Zad Quarter	0	В	Student	A-	A	B-	<u>t</u>	B+	B+ [B	B+ .	A	B-	B÷	 [² 4	В	B+	В	В	A	В	В	B+ [<u></u>	В	<u></u>
Ma	lst Quarter	1																									
	93isogmo)	9/	85	99	85	06	88	16	78	74	7.1	82	06	74	78	74	92	92	56	95	43	92	33	95	1 9/	69	14th panel (15mg
1s s)	Total Arithmetic		59	16	89	56	84	93	93	£9	54	06	75	65	70	65	87	86	32	98	70	84	48	95	77	65	
Basic Skills tile Scores)	Arithmetic Problems	امرا	55	96	94	37	88	96	96	74	44	89	92	65	67	89	85	94	30	81	89	89	55	66	85	79	
Test of 4 (Percen	Arithmetic Concepts		65	75	92	72.	79	83	84	09	57	88	74	92	81	57	89	66	36	88	41	74	41	74	29	47	
Iowa Form	Reading Comprehension	92	87	51	98	98	99	95	71	49	99	75	76	75	09	62	62	06	73	94	33	98	33	91	73	57	
	dubject (Students)		2	က	4	5	9	7	_∞	6	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	



BIBLIOGRAPHY



- American Association for the Advancement of Science. Science—a process approach. (Third Experimental Edition).

 AAAS Commission on Science Education, 1965.
- Baker, Frank. Test Analysis Package: A Program for the CDS

 1604-3600 Computers. Laboratory of Experimental Design,

 Department of Educational Psychology, University of Wisconsin,

 1966.
- Bergamini, David and the Editor of Life. <u>Mathematics</u>. New York: Time, 1963, pp. 130, 133.
- Bloom, Benjamin S. "Learning for Mastery." <u>UCLA CSEIP Evaluation</u>
 <u>Comment.</u> Los Angeles: Center for the Study of Evaluation
 of Instructional Programs, Vol. 1, No. 2, 1968.
- Bruner, Jerome S. The Process of Education. New York: Vintage Books, 1960.
- Buck, R. Creighton. Goals for Mathematics Instruction. The American Mathematical Monthly, LXXII, 1965, pp. 949-956.
- Cambridge Conference on School Mathematics. Goals for School Mathematics. New York: Houghton Mifflin Company, 1963, pp. 70-72.
- Cambridge Conference on School Mathematics. "Report of the 1965 Summer Study." Unpublished mimeograph report, May, 1966, Section II-Chapter 4.
- Cohen, John and Hansel, C. E. M. <u>Risk and Gambling</u>. London: Longmans Green, 1956.
- Cohen, John. Subjective Probability. Scientific American, 1957, 197: 128-138.
- Cohen, John, Dearnaley, E. J. and Hansel, C. E. M. "Measures of Subjective Probability. <u>British Journal of Psychology</u>, 1957, 48: 271-275.
- Cohen, John. Chance, Skill and Luck: The Psychology of Guessing and Gambling. Baltimore: Penguin Books, 1960.
- Commission on Mathematics College Entrance Examination Board.

 <u>Program for College Preparatory Mathematics</u>. New York:
 College Entrance Examination Board, 1959.
- Commission on Mathematics College Entrance Examination Board.

 Introductory Probability and Statistical Inference, An

 Experimental Course. Princeton: Educational Testing
 Service, 1959.



- Davies, C. M. "Development of the Probability Concept in Children." Child Development, 1965, 36: pp. 779-788.
- Doherty, Joan. "Levels of Four Concepts of Probability Possessed by Children of Fourth, Fifth and Sixth Grades Before Formal Instruction." Unpublished Ph.D. dissertation, University of Missouri, 1965.
- Educational Research Council of Greater Cleveland. Greater Cleveland Mathematics Program, Units 1-12. Chicago: Science Research Associates, 1964.
- Eichoiz, Robert E., O'Daffer, Phares, G. <u>Elementary School Mathematics</u>, <u>Book 1, 2, 3</u>. Palo Alto: Addison-Wesley Publishing Company, 1963.
- Eichoiz, Robert E., O'Daffer, Phares, G. <u>Elementary School Mathematics</u>, <u>Book 4, 5, 6</u>. Palo Alto: Addison-Wesley Publishing Company, 1964.
- Engel, A. "Mathematical Research and Instruction in Probability Theory." Mathematics Teacher, Vol. 8, December, 1966, pp. 771-782.
- Flavell, John H. The Developmental Psychology of Jean Piaget. Princeton: D. Van Nostrand Company, Inc., 1963.
- Gagné, Robert M. The Conditions of Learning. New York: Holt, Rinehart and Winston, 1965.
- Gagné, Robert M. "The Acquisition of Knowledge." Research In

 Mathematics Education. Washington, D. C.: National Council of
 Teachers of Mathematics, 1967.
- Gleason, Andrew. "The Interface of Science and Mathematics." The Continuing Revolution in Mathematics. Washington, D. C.:
 National Council of Teachers of Mathematics, 1968, pp. 118-128.
- Girard, Ruth A. "Development of Critical Interpretation of Statistics and Graphs." The Arithmetic Teacher, Vol. 14, April, 1967, pp. 272-277.
- Goldberg, Susan. "Probability Judgments by Preschool Children." Child Development, Vol. 37, 1966, pp. 157-167.
- Grass, Benjamin A. "Statistics Made Simple." The Arithmetic Teacher, Vol. 12, March, 1965, pp. 196-198.
- Hartung, Maurice, Van Engen, Henry, Gibb, E. G., Stochol, James, Knowles, L. and Walch, R. <u>Seeing Through Arithmetic 6</u>. Chicago: Scott, Foresman and Company, 1968.



- International Conference on the Teaching of Probability and Statistics at the Pre-College Level. "Recommendations." Unpublished paper resulting from First CSMP International Conference at Southern Illinois University at Carbondale, Illinois, March 18-27, 1969.
- Leake, Lowell. "The Status of Three Concepts of Probability in Children of 7th, 8th, and 9th Grades." Unpublished Ph.D. dissertation, University of Wisconsin, 1962.
- Leffin, Walter. "A Study of Three Concepts of Probability Possessed by Children in the Fourth, Fifth, Sixth and Seventh Grades." Unpublished Ph.D. dissertation, University of Wisconsin, 1968.
- Meserve, B. E. and Sobel, M. A. <u>Mathematics for Secondary School</u>
 Teachers. Englewood Cliffs, New Jersey: Prentice-Hall, 1962.
- Newman, J. The World of Mathematics. New York: Simon and Schuster Company, 1956.
- Nichols, Eugene D., Flournoy, Frances, Kalin, Robert, Simon, Leonard.

 <u>Elementary Mathematics, Patterns And Structure</u>, <u>Books 1-6</u>.

 New York: Holt, Rinehart and Winston, Inc., 1966.
- Ojemann, Ralph, Maxey, E. J. and Snider, B. C. Effects of a Program of Guided Learning Experiences in Developing Probability Concepts at 3rd Grade. <u>Journal of Experimental Education</u>, 1965, 33: 321-330.
- Ojemann, Ralph, Maxey, E. J. and Snider, B. C. Effects of Guided Learning Experiences in Developing Probability Concepts at the Fifth Grade Level. Preceptional and Motor Skills, 1965, 415-427.
- Ott, Ellis R. "Statistics an Enigma." Extracts from paper presented at the Annual Conference of the National Council of Teachers of Mathematics, Philadelphia, Pennsylvania, April 19, 1968.
- Page, David A. "Probability." The Growth of Mathematical Ideas,
 Grades K-12. Twenty-Fourth Yearbook of the National Council of
 Teachers of Mathematics. Washington, D. C.: NCTM, 1959,
 pp. 229-271.
- Payne, Joseph N., Spooner, George A., Clark, Caroline H., Beatty, Leslie S., Wells, David W. <u>Elementary Mathematics</u>. New York: Harcourt, Brace and World, Inc., 1966.
- Popham, W. James and Huskek, T. R. "Implications of Criterion-Referenced Measurement." <u>Journal of Educational Measurement</u>, 1969, Vol. 6, No. 1, pp. 1-9.





- Price, G. Bailey. "Progress in Mathematics and Its Implication for the Schools." The Revolution in School Mathematics. Washington D. C.: The National Council of Teachers of Mathematics, 1961, p. 8.
- Rade, Lennart. "A Course in Probability Theory for Secondary Schools."

 <u>Mathematics Teacher</u>, Vol. 12, October, 1965, pp. 528-535.
- Romberg, Thomas A. "Curriculum Research and Development." The Teaching of Mathematics. Thirty-fourth Yearbook of the National Council of Teachers of Mathematics. Washington, D. C.: The Council, To be published.
- Remberg, Thomas and DeVault, Vere. "Mathematics Curriculum: Needed Research." Journal of Research and Development in Education, Vol. 1, No. 1, Fall, 1967. Athens: The University of Georgia, 1967.
- School Mathematics Study Group. <u>Introduction to Probability, Part I Basic Concepts</u>. Palo Alto, California: Stanford University Press, 1966.
- School Mathematics Study Group. <u>Introduction to Probability</u>, <u>Part II Special Topics</u>. Palo Alto, California: Stanford University Press, 1966.
- School Mathematics Study Group. <u>Probability for Primary Grades</u>. Palo Alto, California: Stanford University Press, 1966.
- School Mathematics Study Group. <u>Probability for Intermediate Grades</u>. Palo Alto, California: Stanford University Press, 1966.
- Secondary School Curriculum Improvement Study. <u>Unified Modern</u>

 <u>Mathematics Course I, Part I.</u> New York: Teachers College,
 Columbia University, 1967, pp. 246-287.
- Shepler, Jack L. An Exploratory Study of the Interaction of Three Elementary Concepts of Probability with Stimuli, Socioeconomic, Grade and IQ Differences." Technical Report from the Research and Development Center for Cognitive Learning, University of Wisconsin, 1969, in preparation.
- Shepler, Jack L., Harvey, John G., Romberg, Thomas A. "A Proposal and Task Analysis for Teaching Probability and Statistics Concepts in the Elementary School." Working Paper from the Research and Development Center for Cognitive Learning, University of Wisconsin, 1969, in preparation.



- Smith, Malcom. "Development and Preliminary Evaluation of a Unit on Probability and Statistics at the Junior High School Level." Unpublished Ph.D. dissertation, University of Georgia, 1966.
- Sullivan, Edmund V. <u>Piaget and the School Curriculum--A Critical Appraisal</u>. Toronto: The Ontario Institute for Studies in Education, Bulletin No. 2, 1967, p. 33.
- Suppes, Patrick, Kyser, Dolly and Braithwaite, Catherine. <u>Sets and Numbers</u>, <u>Books 4</u>, <u>5</u>, <u>and 6</u>. New York: Singer Company, Inc., 1966.
- Walbesser, Henry. "An Evaluation Model and Its Application Second Report." <u>Science--A Process Approach</u>. Miscellaneous Publication 68-4, AAAS Commission on Science Education, 1968.
- Wilkinson, J. D. and Nelson, O. "Probability and Statistics: Trial Teaching in 6th Grade." The Arithmetic Teacher, Vol. 13, February, 1966, pp. 100-106.
- Yost, Patricia A., Siegel, A. and Andrews, J. "Nonverbal Probability Judgements by Young Children." Child Development, 1962, Vol. 33 pp. 769-780.

